

# CoE-MaSS weekly seminar series

THE DST-NRF CENTRE OF EXCELLENCE IN MATHEMATICAL AND  
STATISTICAL SCIENCES (CoE-MaSS) WOULD LIKE TO PRESENT  
A SEMINAR BY

**Florian Luca**

*(School of Mathematics, Wits University)*

*“Diophantine  $m$ -tuples”*

Friday, 12 February 2016  
10h30-11h30



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**Broadcast live from:**

Videoconferencing Facility, 1st Floor  
Mathematical Sciences Building, Wits West Campus

**How to connect to this seminar remotely:**

You can connect remotely via Vidyo to this research seminar by clicking on this link:  
<http://wits-vc.tenet.ac.za/flex.html?roomdirect.html&key=y0SSOwFsvsidbzig4qFdWXvvQtyl>  
and downloading the Vidyo software before the seminar.

You must please join in the virtual venue (called “CoE Seminar Room (Wits)” on Vidyo)  
strictly between **10h00-10h15**. No latecomers will be added.

**Important videoconferencing netiquette:**

Once the seminar commences, please mute your own microphone so that there is no feedback from your side into the virtual room. During the Q&A slot you can then unmute your microphone if you have a question to ask the speaker.

**Title:**

Diophantine  $m$ -tuples

**Presenter:**

Florian Luca, School Mathematics, University of the Witwatersrand, Johannesburg, South Africa; [Florian.Luca@wits.ac.za](mailto:Florian.Luca@wits.ac.za)

**Abstract:**

A diophantine  $m$ -tuple is a set of  $m$ -positive integers  $\{a_1, \dots, a_m\}$  such that the product of any two of them plus 1 is a square. For example,  $\{1, 3, 8, 120\}$  is a Diophantine quadruple found by Fermat. It is known that there are infinitely many such examples with  $m = 4$  and none with  $m = 6$ . No example is known with  $m = 5$  but if there exist, then there are only finitely many such. In my talk, I will survey what is known about this problem, as well as its variations, where one replaces the ring of integers by the ring of integers in some finite extension of  $\mathbf{Q}$ , or by the field of rational numbers, or one looks at a variant of this problem in the ring of polynomials with coefficients in a field of characteristic zero, or when one replaces the squares by perfect powers of a larger exponent, or by members of some other interesting sequence like the sequence of Fibonacci numbers and so on.

